

## CRYSTAL FIELD INTERACTIONS OF “LARGE” ROTORS EMBEDDED IN SOLID PARAHYDROGEN (BRIEFING CHARTS AND ABSTRACT)

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### BRIEFING CHARTS AND ABSTRACT

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# Crystal Field Interactions of “Large” Rotors Embedded in Solid Parahydrogen

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# Rotation in the Solid Matrices

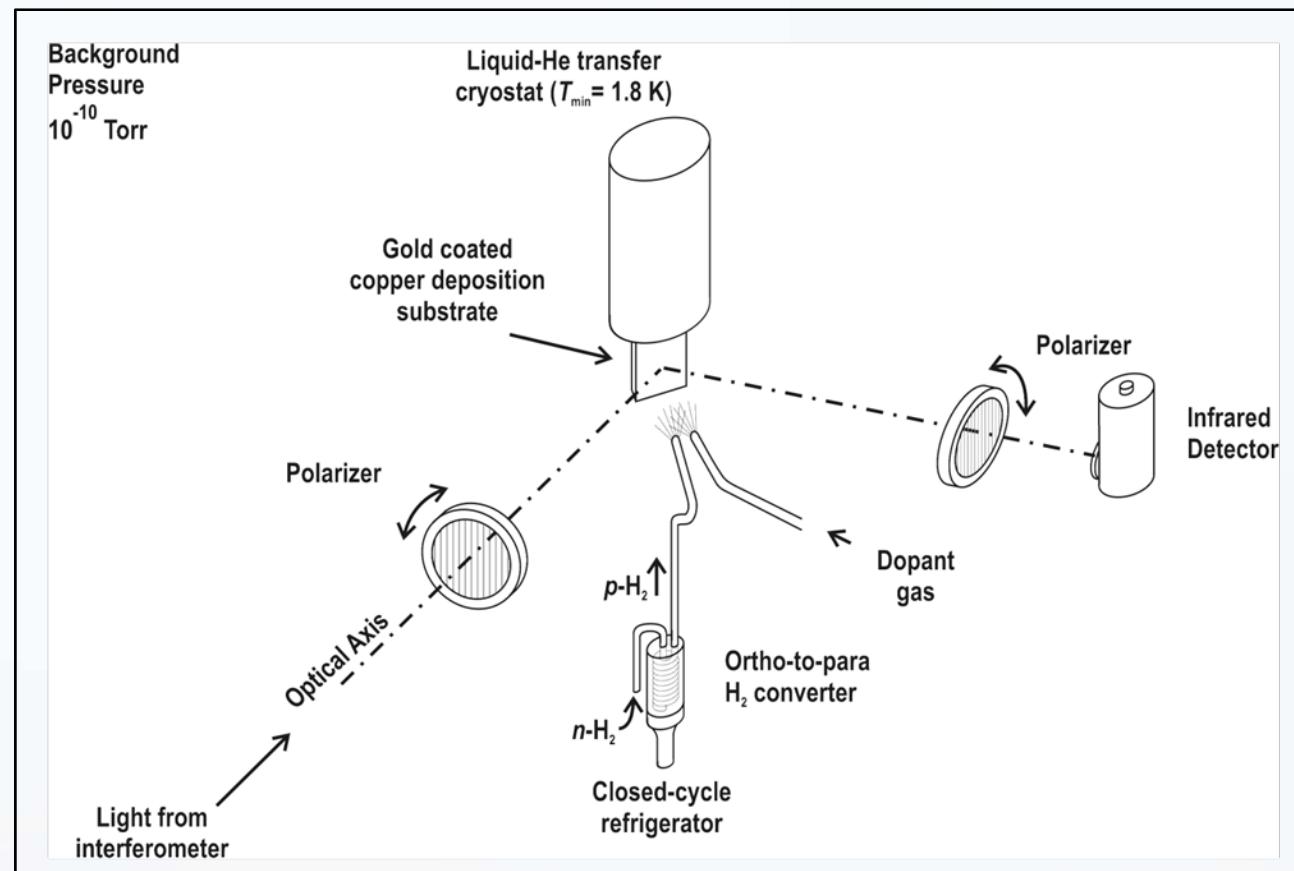
- Rare gas matrices and traditional molecular matrices:
  - Small hydrides: HX, H<sub>2</sub>O, NH<sub>2</sub>, NH<sub>3</sub>, CH<sub>3</sub>, CH<sub>4</sub>
  - *Perhaps* CIF, CN (ESR and IR spectra conflict)
  - fcc lattice structure
- Solid Parahydrogen:
  - Very low angular anisotropy, and weak intermolecular interactions
  - Small hydrides: HX, H<sub>2</sub>O, NH<sub>3</sub>, CH<sub>3</sub>, CH<sub>4</sub>
  - “Large” molecules: N<sub>2</sub>, O<sub>2</sub>, CO, HCN, ... *more?*
  - fcc (as deposited) and hcp (annealed) lattice structure

**Narrow spectral lines widths and the ability to examine the rotation of larger molecules allows us to examine the impurity-matrix interactions with remarkable clarity**



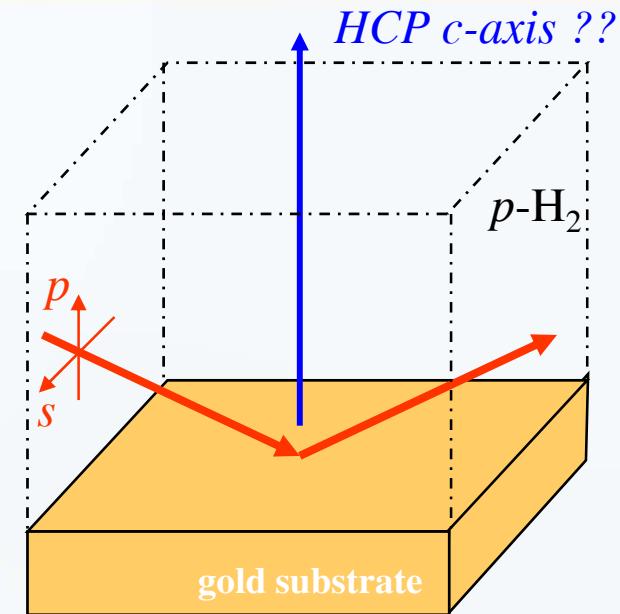
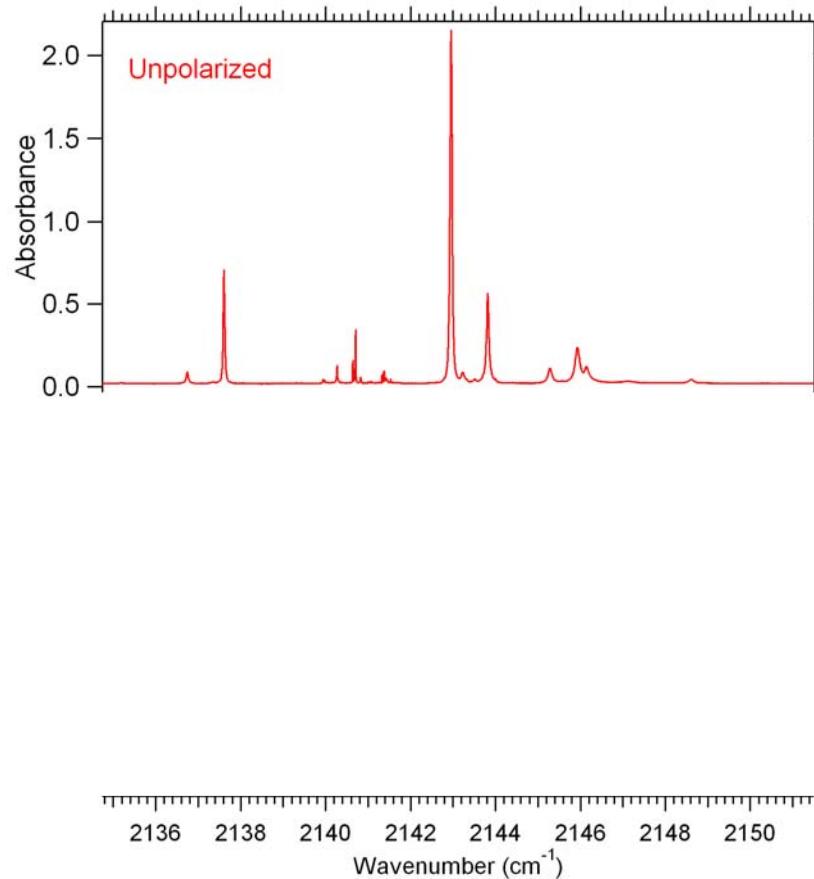
# Rapid vapor deposition of p-H<sub>2</sub>

- Reflection based set-up (FTIR).
- $[o\text{-H}_2] < 100 \text{ ppm}$ .
- $p\text{-H}_2$  deposition rate  $\sim 150 \text{ mmol/hr} \rightarrow \sim 1 \text{ mm/hr}$  thickness.
- Deposition at 2.3 K. Sample annealed at 4.3 K for 30 min.





# Polarization Spectroscopy

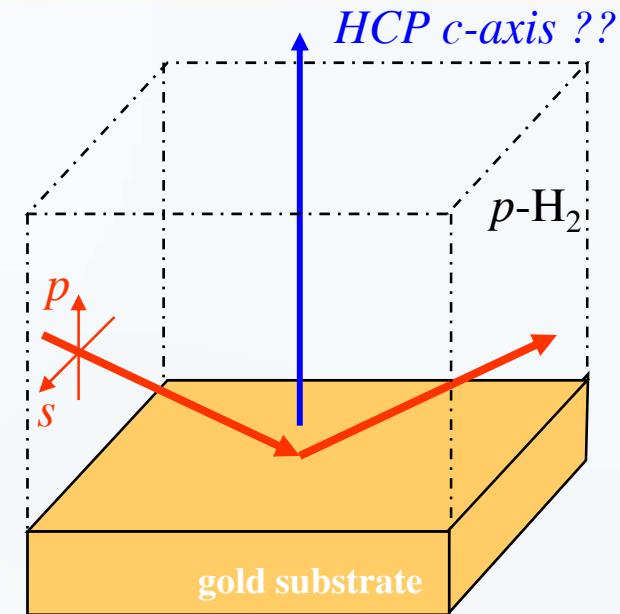
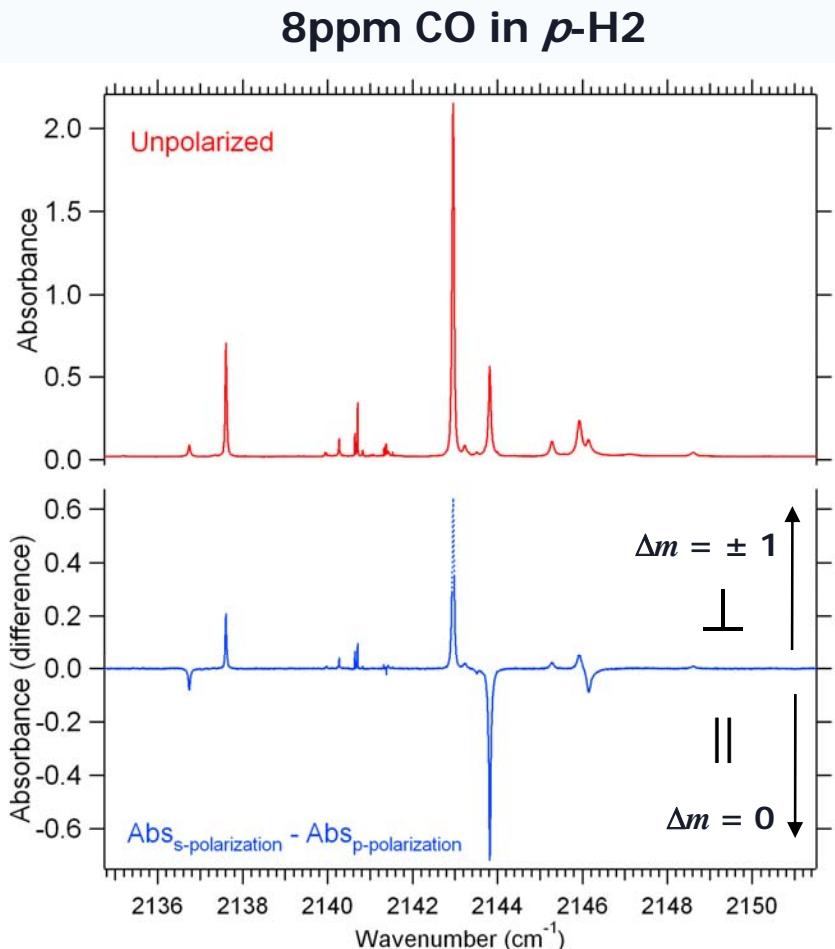


## Polarization analysis provides:

- An assignment of the perpendicular and parallel components to the crystal field perturbed rotational structure (*i.e.*  $\Delta m$ )
- $\text{Abs}_{\text{s-pol}} - \text{Abs}_{\text{p-pol}} = \frac{1}{2} \mu^2_{\perp} - \frac{1}{2} \mu^2_{\parallel}$



# Polarization Spectroscopy

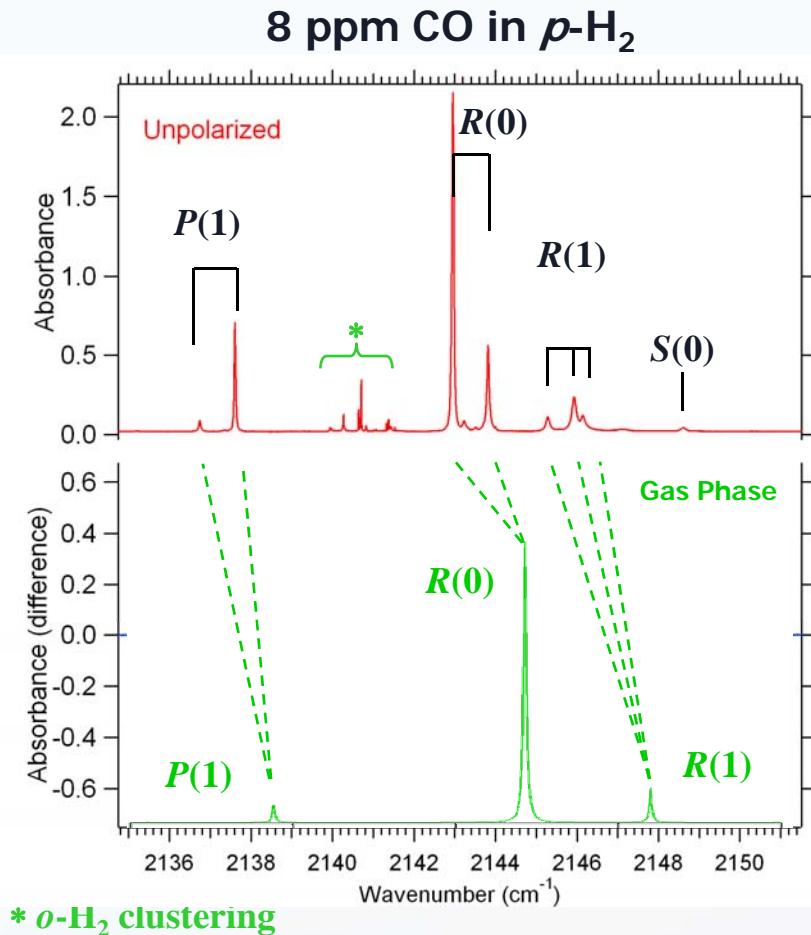


## Polarization analysis provides:

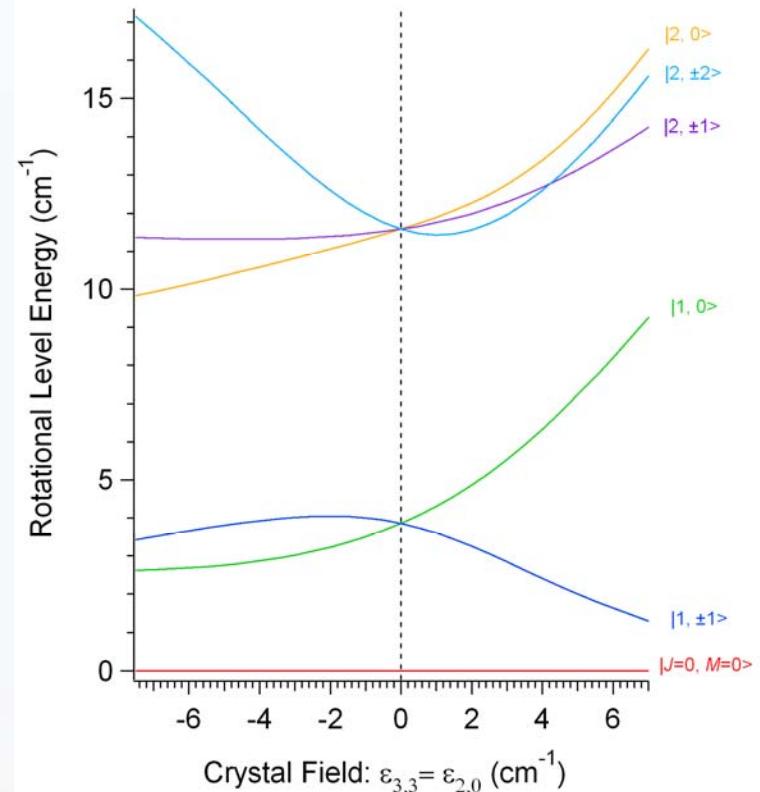
- An assignment of the perpendicular and parallel components to the crystal field perturbed rotational structure (*i.e.*  $\Delta m$ )
- $\text{Abs}_{\text{s-pol}} - \text{Abs}_{\text{p-pol}} = \frac{1}{2} \mu_{\perp}^2 - \frac{1}{2} \mu_{\parallel}^2$



# Rotation in parahydrogen



Simulation:  
Linear molecule in *h.c.p* crystal field



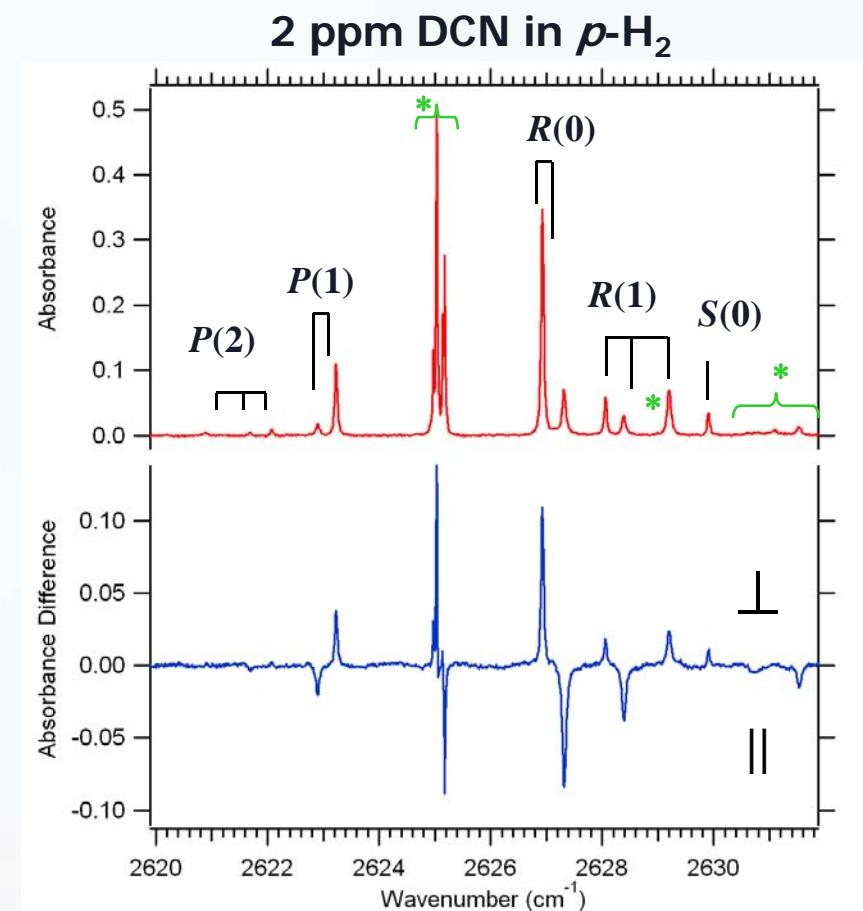
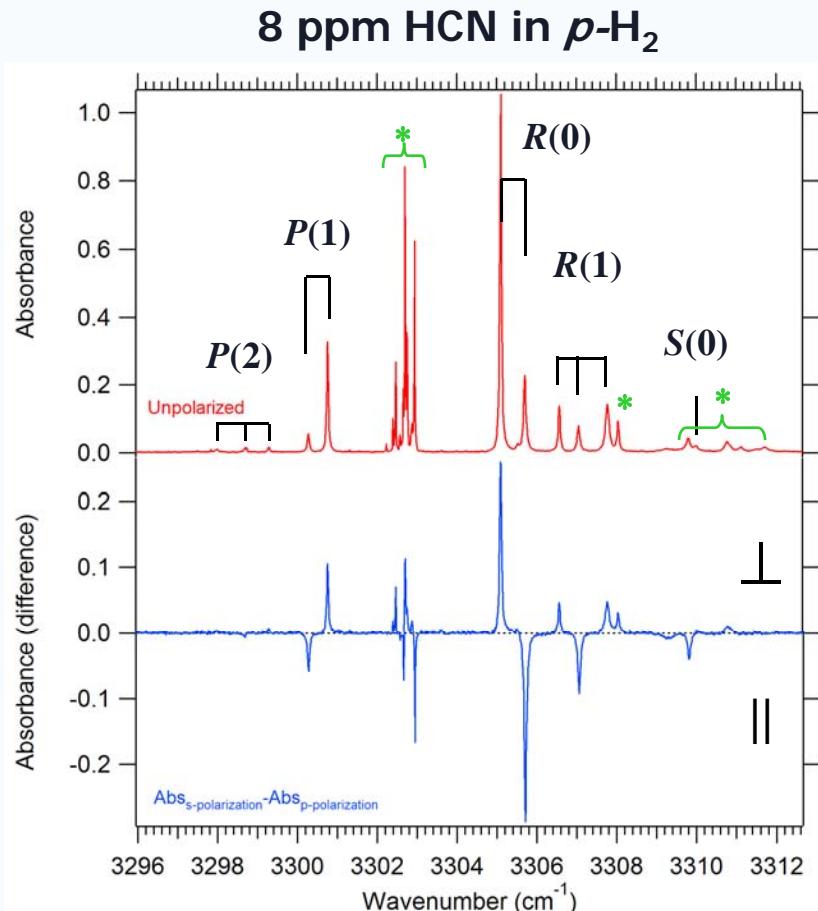
Simulation uses theory of: Devonshire, Proc. Roy. Soc. London A 153, 601 (1936);

Bowers and Flygare, J. Chem. Phys., 44, 1389 (1966).

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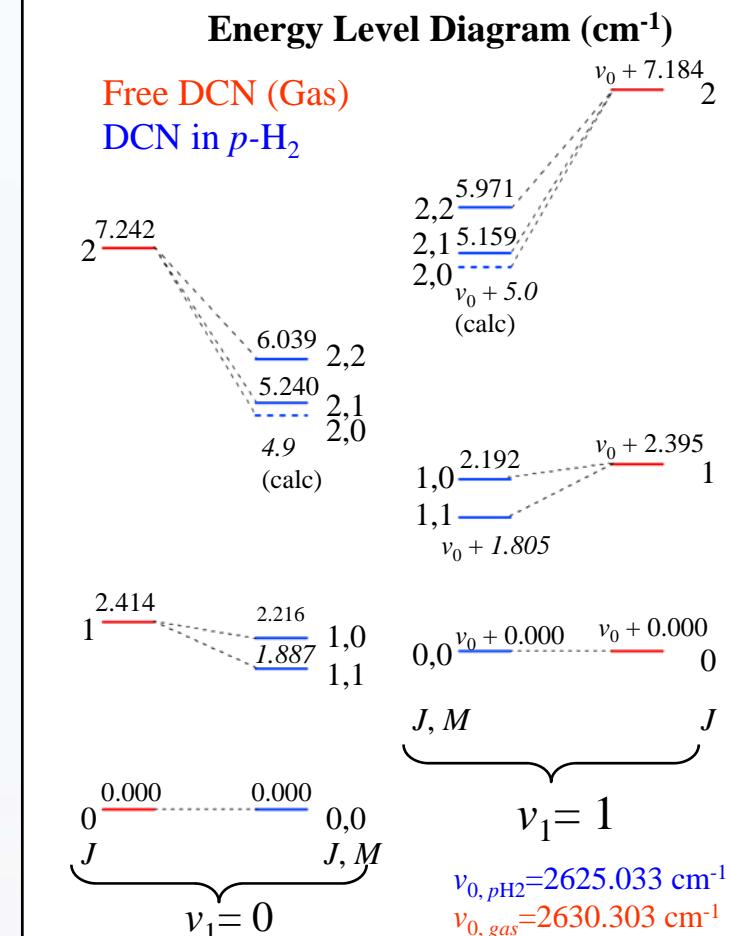
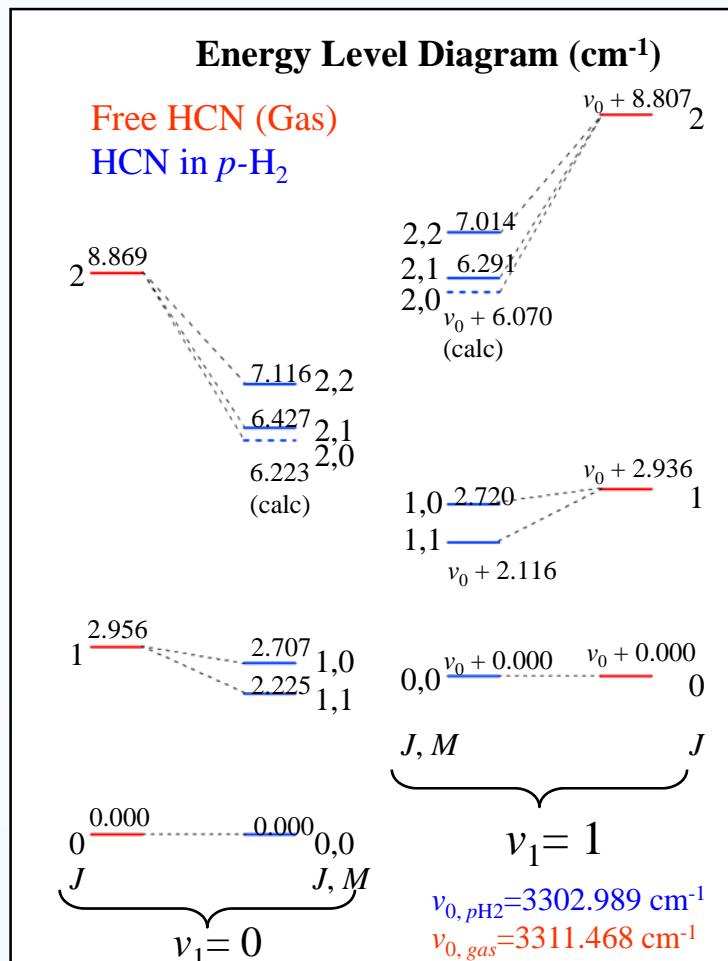


# HCN in parahydrogen

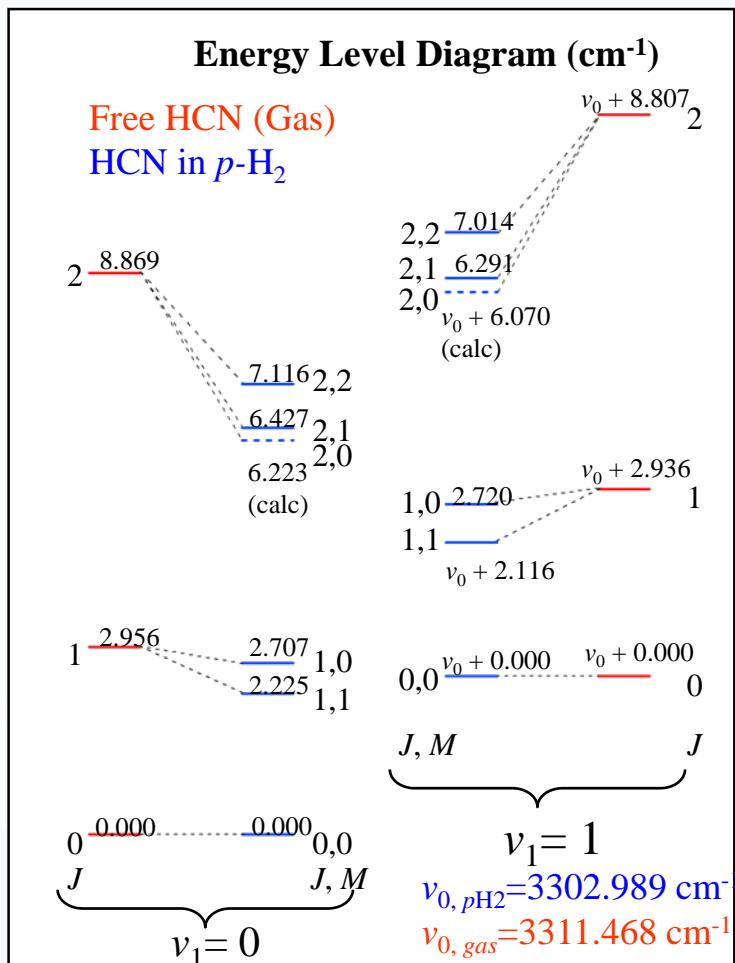


\*  $o\text{-H}_2$  clustering

# HCN/DCN Energy Level Diagrams



# Interpretation of the Rotational Fine Structure- HCN + DCN



Crystal field theory (linear molecule in HCP lattice) \*

$$H = H_{\text{r,v}} + V_{\text{cry}}$$

$$V_{\text{cry}} = \varepsilon_2 C_{2,0}(\Omega_{\text{HCN}}) + \varepsilon_3 [C_{3,-3}(\Omega_{\text{HCN}}) - C_{3,3}(\Omega_{\text{HCN}})]$$

$$\text{where } C_{l,m}(\Omega) = \left( \frac{4\pi}{2l+1} \right)^{\frac{1}{2}} Y_{l,m}(\Omega)$$

“Fitting” Results in  $\text{cm}^{-1}$ : (10 levels, 9 parameters)

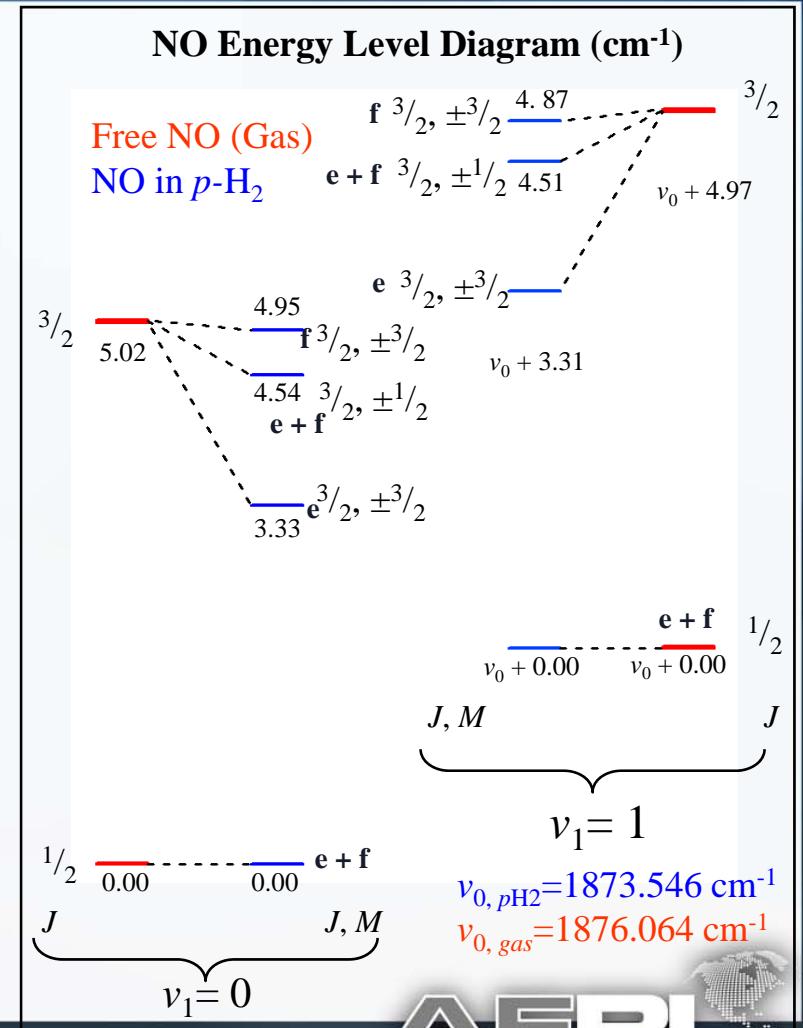
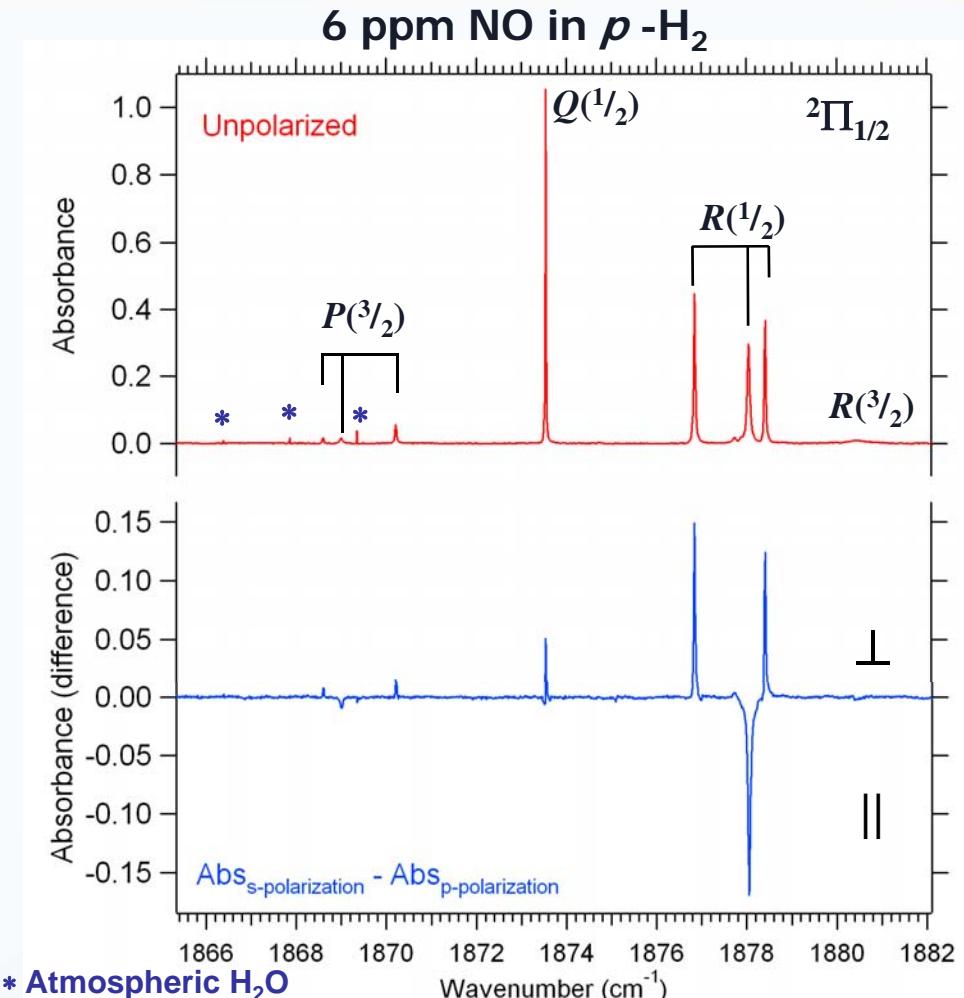
	HCN		DCN	
	$p\text{-H}_2$	Gas	$p\text{-H}_2$	Gas
$B$	1.475(5)	1.478	1.2791(5)	1.207
$\Delta B$	-0.005(5)	-0.010	-0.032(5)	-0.010
$D$	0.0675(5)	$2.910 \times 10^{-6}$	0.0654(5)	$1.927 \times 10^{-6}$
$\Delta D$	0.0032(5)	$0.025 \times 10^{-6}$	-0.0028(5)	$0.017 \times 10^{-6}$
$v_0$	3302.989(5)	3311.4770	2625.093(10)	2630.3033
$\varepsilon_2$	-1.274(5)	-	-2.142(5)	-
$\Delta \varepsilon_2$	-0.193(5)	-	-0.047(5)	-
$\varepsilon_3$	6.850(5)	-	7.500(5)	-
$\Delta \varepsilon_3$	0.767(5)	-	0.028(5)	-

very large!  $\times 20,000!$  Identical!

NOTE: Above perturbation does not converge for large  $D$ !  
Treatment was modified to incorporate centrifugal distortion after crystal field calculation to avoid this problem.

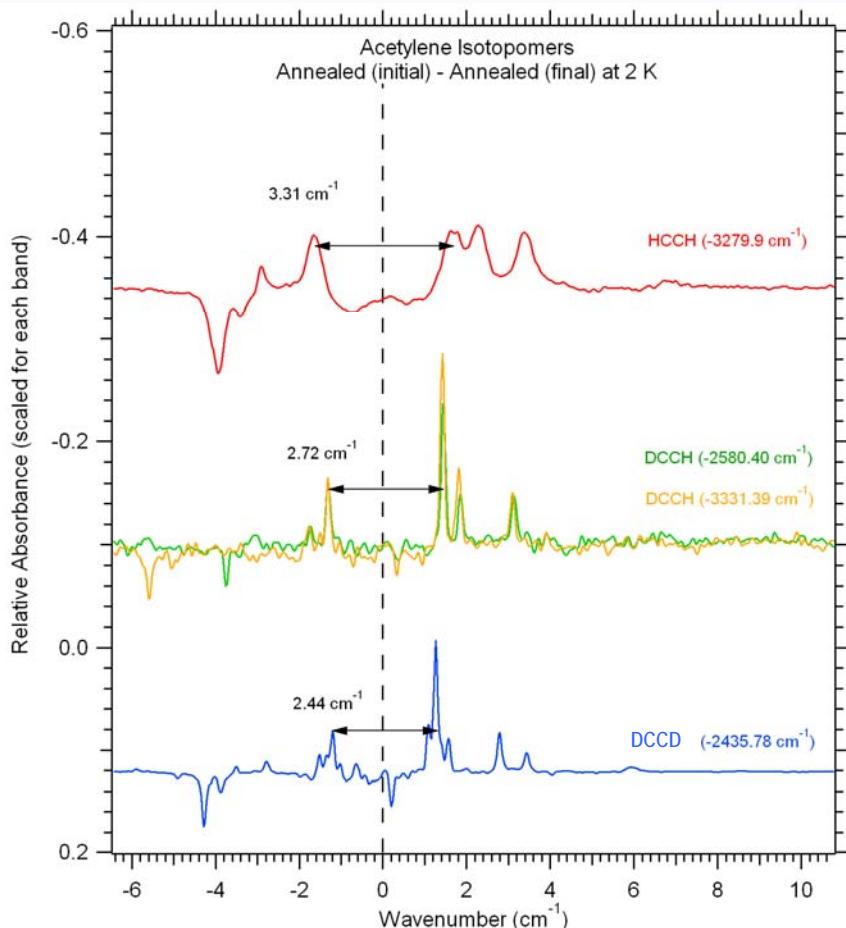


# NO in Solid Parahydrogen





# Preliminary C<sub>2</sub>H<sub>2</sub> in parahydrogen



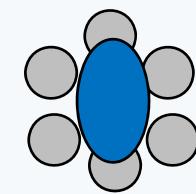
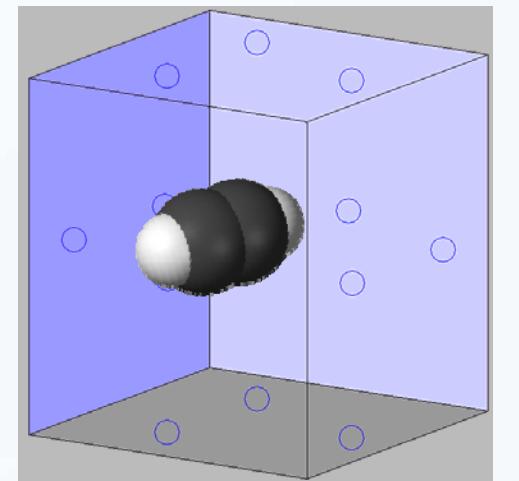
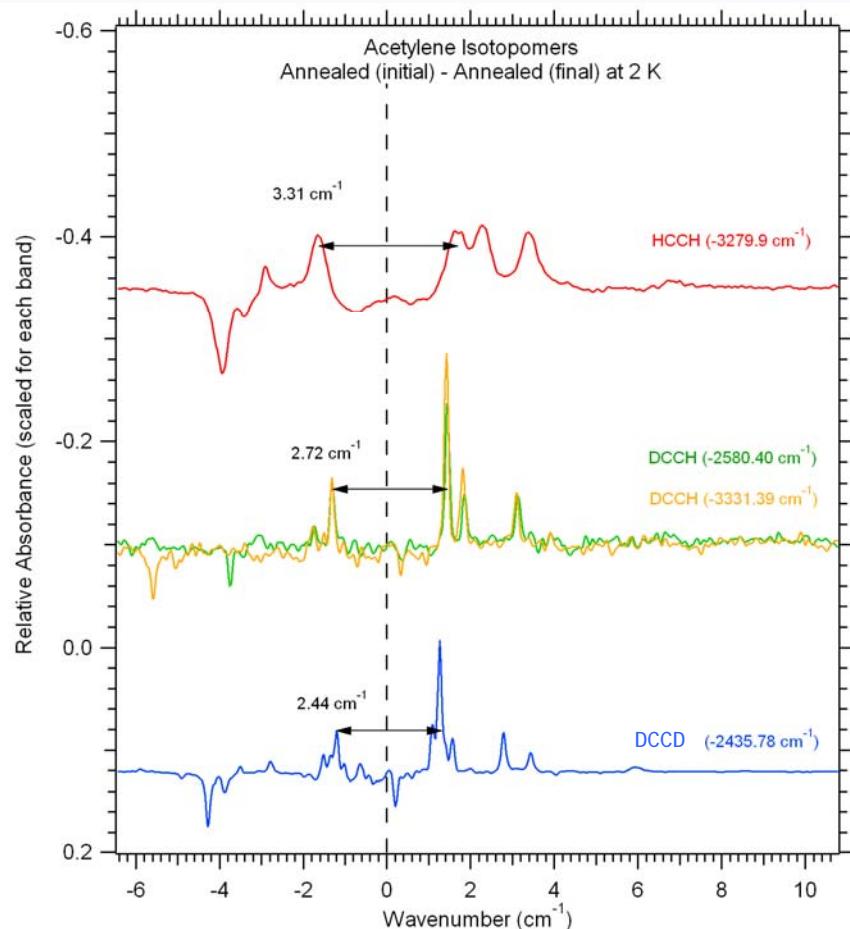
$E_{R(0)} - E_{P(1)}$ (4B)		$p\text{H}_2$		
Gas		$p\text{H}_2$		
Wavenumber	Relative	Wavenumber	Relative	
HCCH	4.71 cm <sup>-1</sup>	<b>1.00</b>	3.35 cm <sup>-1</sup>	<b>1</b>
DCCH	3.97 cm <sup>-1</sup>	<b>0.84</b>	2.74 cm <sup>-1</sup>	<b>0.82</b>
DCCD	3.39 cm <sup>-1</sup>	<b>0.72</b>	2.47 cm <sup>-1</sup>	<b>0.74</b>

- Acetylene IR spectrum 'ages'... timescale of 30 minutes. Aging appears to be acetylene-acetylene clustering.
- "Rotational spectrum" disappears fairly quickly (but not with annealing!)

Y.P. Lee and collaborators *Chem. Phys. Lett.* **435** 247-251 (2007) – no rotation at 'high' [o-H<sub>2</sub>]



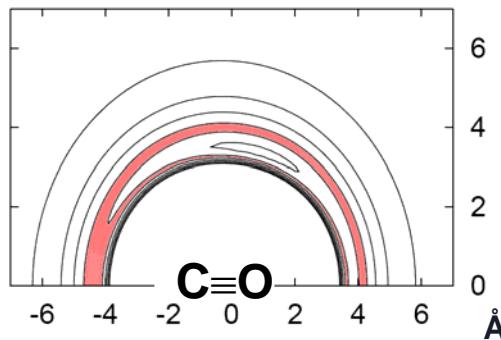
# Preliminary C<sub>2</sub>H<sub>2</sub> in parahydrogen



- HCCH Van der Waal diameter  $\sim 6.4 \text{ \AA}$
- $p\text{-H}_2$  intermolecular spacing –  $3.8 \text{ \AA}$
- Substantial overlap of wavefunctions

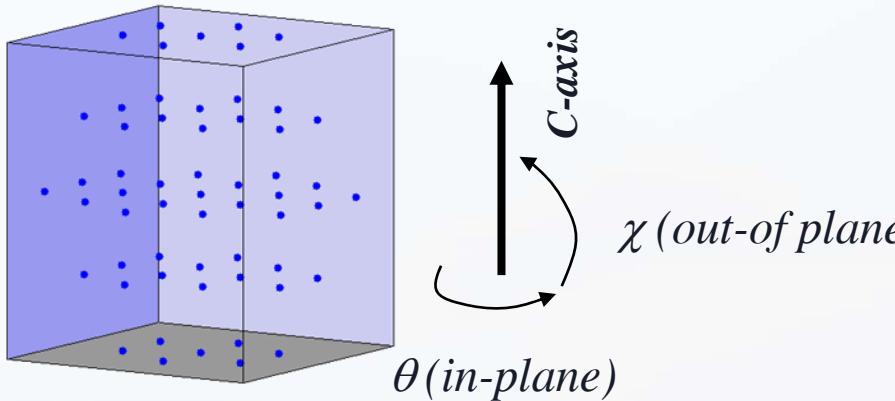
# Prediction of Crystal Field Parameters: Truncation

## Pair Potential

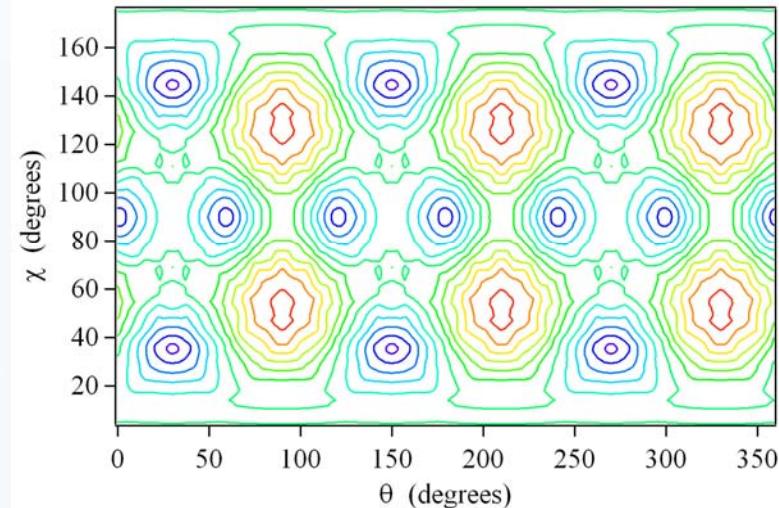


+

$\text{H}_2 - \text{h.c.p. lattice}$



## Rotational PES dopant in $\text{h.c.p}$ $\text{H}_2$ lattice (Rigid)



Crystal field theory (linear molecule in HCP lattice) \*

$$H = H_{\text{r,v}} + V_{\text{cry}}$$

$$V_{\text{cry}} = \sum_{l,m} \varepsilon_{l,\pm m} \left( \frac{4\pi}{2l+1} \right)^{1/2} Y_{l,\pm m}(\Omega)$$

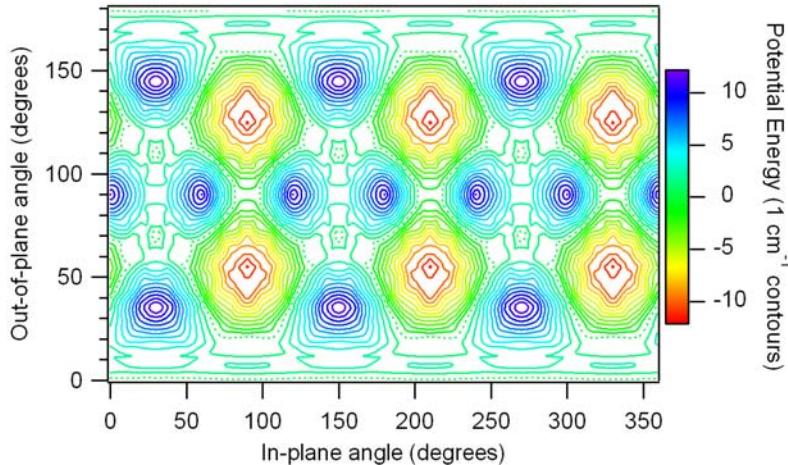
\* SAPT/MC<sup>+</sup>BS, P. Jankowski and K. Szalwicz, *J. Chem. Phys.* **108**, 3554 (1998).

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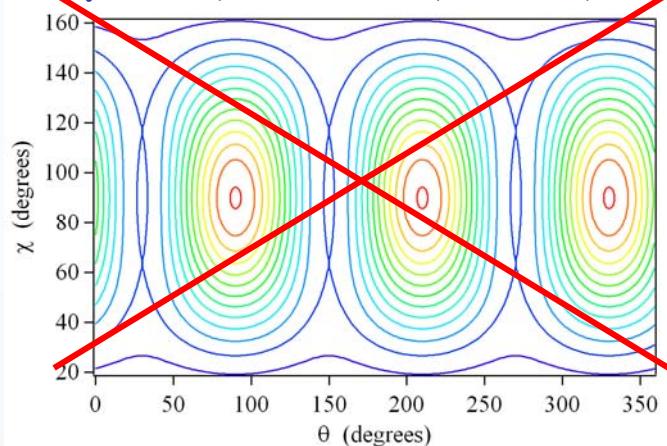


# Prediction of Crystal Field Parameters: Truncation - CO

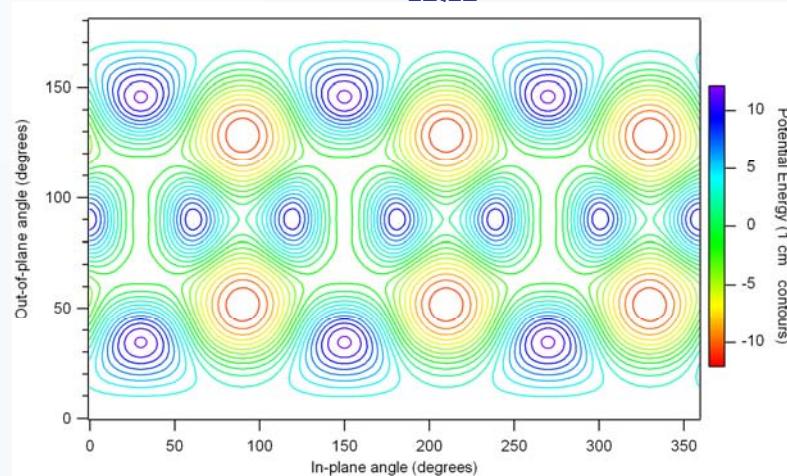
Rotational PES for CO



$$V_{\text{cry}} = \varepsilon_2 C_{2,0}(\Omega) + \varepsilon_3 [C_{3,-3}(\Omega) - C_{3,3}(\Omega)]$$



CFT -up to  $C_{12,12}(\Omega)$



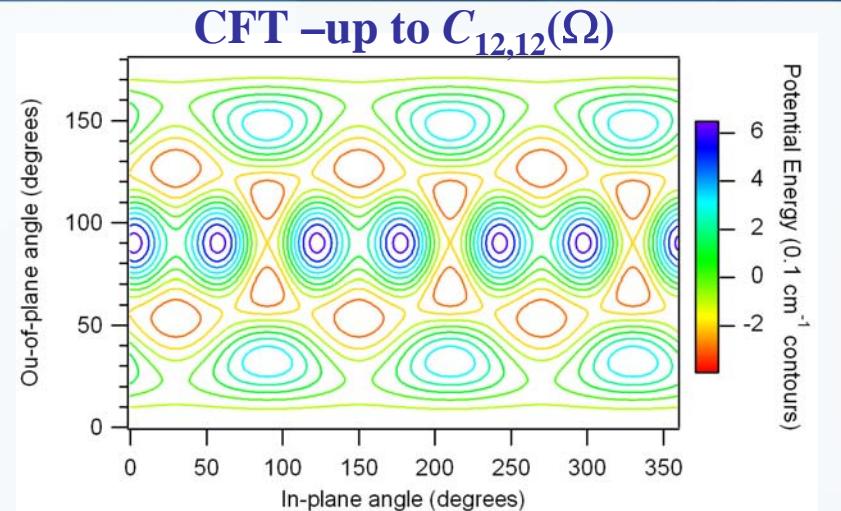
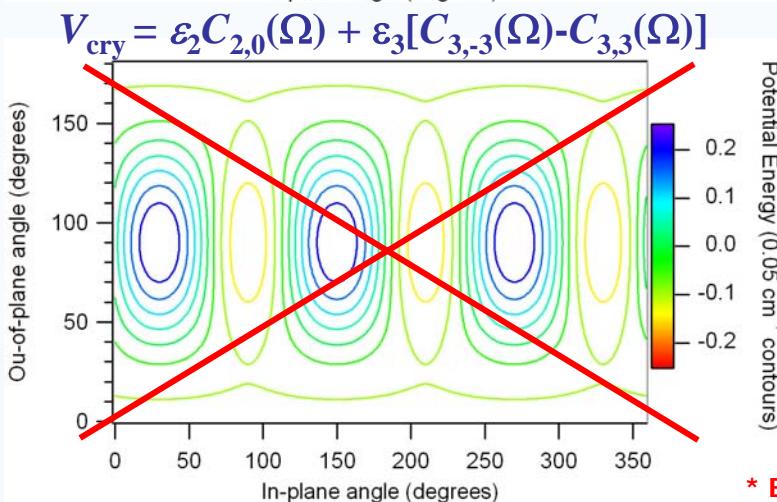
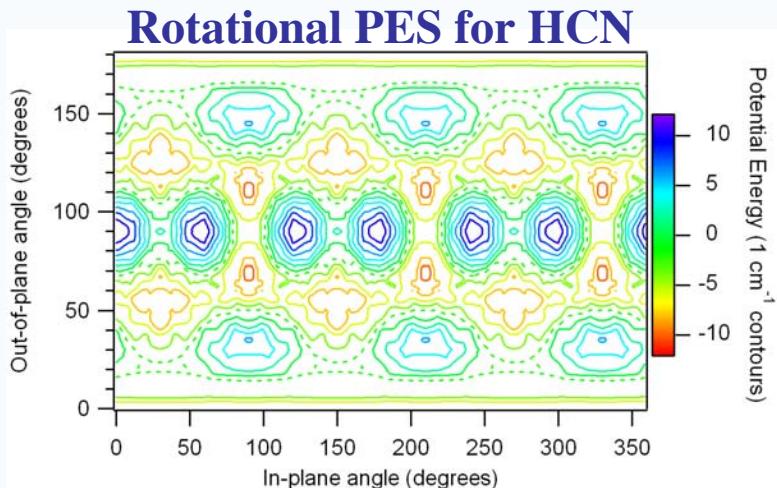
(2.52)\*

$\varepsilon$ (cm⁻¹)	Term	$\varepsilon$ (cm⁻¹)	Term
4.86	$C_{3,3}(\Omega)$	0.65	$C_{9,3}(\Omega)$
6.74	$C_{5,3}(\Omega)$	0.55	$C_{12,6}(\Omega)$
6.54	$C_{4,0}(\Omega)$	0.46	$C_{8,0}(\Omega)$
3.68	$C_{6,6}(\Omega)$	0.43	$C_{12,12}(\Omega)$
-5.80	$C_{6,0}(\Omega)$	-0.02	$C_{12,0}(\Omega)$
2.61	$C_{7,3}(\Omega)$	-0.47	$C_{11,3}(\Omega)$
1.10	$C_{8,6}(\Omega)$	-0.22	$C_{2,0}(\Omega)$

\* Experimentally fitted values.

(1.03)\*

# Prediction of Crystal Field Parameters: Truncation - HCN



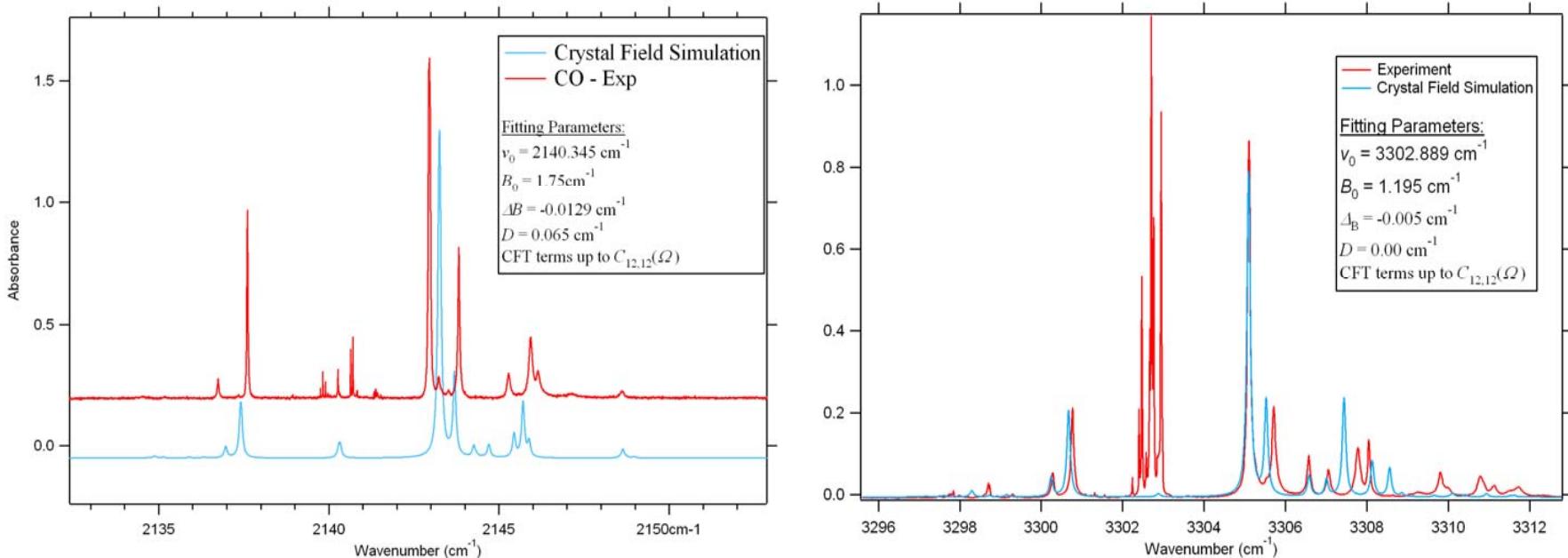
$\varepsilon$ ( $\text{cm}^{-1}$ )	Term	$\varepsilon$ ( $\text{cm}^{-1}$ )	Term
-3.04	$C_{6,6}(\Omega)$	0.63	$C_{8,6}(\Omega)$
-2.28	$C_{5,3}(\Omega)$	0.09	$C_{8,0}(\Omega)$
3.35	$C_{4,0}(\Omega)$	-0.01	$C_{9,3}(\Omega)$
-4.82	$C_{6,0}(\Omega)$		
0.70	$C_{3,3}(\Omega)$		
-1.24	$C_{7,3}(\Omega)$		
-0.47	$C_{2,0}(\Omega)$		
<b>(6.85/7.50)*</b>		<b>(-1.27/-2.14)*</b>	

\* Experimental fitted values for HCN/DCN.

\* HCN-H<sub>2</sub> Pair Potential - D. Moore, unpublished,

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# Estimation of Crystal Field Parameters: Simulated Spectrum for CO + HCN



- Qualitative agreement with experiment
- Overestimates splitting in  $J=1$  manifold – rigid lattice structure
- Underestimates  $\epsilon_{2,0}$  parameter
- Compression of rotational fine structure ( $B_{eff}/D_{eff}$ ) not accounted for by crystal field



# Summary

## Conclusions

- Parahydrogen is remarkably accommodating to rotating molecules... even HCCH!
- “reduction” in rotational constant can be thought as a large centrifugal distortion constant... B may not be affected at all
- Simulations using pair potentials and rigid lattice agree qualitatively with experiment

## Acknowledgements:

- Takamasa Momose (Crystal field theory for CO)
- David Anderson (NO data)
- David Moore ( $H_2$ -HCN potential calculations)



# QUESTIONS?

